

Shivaji Univeristy, Kolhpaur
Question Bank for Mar 2022 (Summer) Examination
Sub Code : 79698 Subject Name : 79698 Statistics Paper IX
Probability Distributions

Q.1 Choose the most correct alternative.

- 1) The ratio of two i.i.d. standard normal variates is _____.
 - i) Laplace
 - ii) Lognormal
 - iii) Cauchy
 - iv) Weibull
- 2) If $X \sim C(0,1)$ then $Y = \tan^{-1}X$ follows
 - i) Laplace
 - ii) uniform
 - iii) Weibull
 - iv) Normal
- 3) If $X \sim W(1,1)$ then distribution function of X is
 - i) $1 + e^x$
 - ii) $1 - e^x$
 - iii) $1 - e^{-x}$
 - iv) e^{-x}
- 4) If X follows logistic distribution with parameters $\mu = 0, \sigma = 1$ then distribution function of X is
 - i) $1 - e^{-x}$
 - ii) $(1 + e^{-x})^{-1}$
 - iii) $(1 - e^{-x})^{-1}$
 - iv) None of these.
- 5) Which of the following is a particular case of Multinomial distribution
 - i) Normal
 - ii) Exponential
 - iii) uniform
 - iv) Trinomial
- 6) If X is a random variable having p.m.f. $P(X) = C \cdot {}^n C_x p^x q^{n-x}$, $X=1, 2, \dots, n$. then the value of C is
 - i) $\frac{1}{(1-q^n)}$
 - ii) $1 - q^n$
 - iii) p^n
 - iv) $1 - p^n$
- 7) If X is truncated exponential variate with parameter Θ truncated to the left below $X = 5$ then mean and variance of X are
 - i) $\frac{1}{\Theta^2}, \frac{5}{\Theta^2}$
 - ii) $\frac{1}{\Theta}, \frac{1}{\Theta^2}$
 - iii) $\frac{1}{\Theta}, \frac{5}{\Theta^2}$
 - iv) $5 + \frac{1}{\Theta}, \frac{1}{\Theta^2}$

35) If $(x, y) \sim \text{BN}(\mu_1, \mu_2, \sigma_1^2, \sigma_2^2, \rho)$ then $U = \left(\frac{x-\mu_1}{\sigma_1} + \frac{y-\mu_2}{\sigma_2} \right)$ follows

- i) $N(0, 1+\rho)$ ii) $N(0, 1-\rho)$
iii) $N(0, 2(1+\rho))$ iv) $N(0, 2(1-\rho))$

36) If x follows Lognormal distribution with parameters (μ, σ^2) then mean of x is

- i) e^{σ^2} ii) $e^{\mu + \frac{\sigma^2}{2}}$
iii) $e^{\sigma^2 + \frac{\mu}{2}}$ iv) e^{μ}

37) If x follows Cauchy distribution with parameters (μ, λ) then coefficient of Q.D. is

- i) $\frac{\lambda}{\mu}$ ii) $\frac{\lambda}{\mu + \lambda}$
iii) $\frac{\mu}{\mu + \lambda}$ iv) None of these.

38) If x follows Logistic distribution with parameters (μ, λ) then the mode of x is

- i) σ ii) μ
iii) $\mu + \sigma$ iv) None of these.

39) Following is the p.m.f. of truncated Poisson distribution, truncated at $x = 0$ $P(x) = c \frac{e^{-m} m^x}{x!}$, $x = 1, 2, \dots$ then the value of C is

- i) m ii) $\frac{1}{m}$
iii) $1 - e^{-m}$ iv) $\frac{1}{1 - e^{-m}}$

40) If $X \sim \text{LN}(5, 4)$ then $E(X)$ is

- i) e^6 ii) e^7
iii) e^5 iv) e^4

41) The median of a Lognormal distribution with parameters μ and σ^2 is

- i) e^{μ} ii) e^{σ^2}
iii) $e^{\mu + \sigma^2}$ iv) None of these.

Q.2 Attempt any 02 questions

8 Marks

- 1) Obtain distⁿ function of Cauchy distⁿ and hence find quartiles.
- 2) Define truncated Binomial distⁿ, truncated to the left at $X = 0$ and obtain its mean & variance.
- 3) Obtain the distribution function of Laplace distⁿ and hence find quartiles.
- 4) Define Multinomial distⁿ and obtain means and variances.
- 5) Define truncated Poisson distⁿ, truncated to the left at $X = 0$ and obtain its mean & variance
- 6) Define Lognormal distribution with parameters (μ, σ^2) . Find its mean and variance.
- 7) If $(X,Y) \sim BN ((\mu_1, \mu_1, \sigma^2, \sigma^2, p))$ then obtain the distribution $aX+bY+c$, where a,b and c are real numbers.
- 8) Obtain distⁿ function of Cauchy distⁿ with parameters (μ, λ) and hence find quartile deviation.
- 9) If $(X,Y) \sim BN ((0,0, \sigma^2, \sigma^2, p))$ then obtain the distribution X/Y
- 10) Obtain first and second raw moments about origin of Lognormal distribution with parameters (μ, σ^2) .
- 11) Define power series distribution. Show that Binomial, Poisson and Geometric distribution are particular cases of power series distribution.
- 12) If $(X,Y) \sim BN ((0,0, \sigma^2, \sigma^2, p))$ then obtain m.g.f. of (X,Y) . Also find $E(X)$ and $E(Y)$.

- 13) Define Pareto distribution and find its mean and variance.
- 14) Obtain mean of truncated normal distribution with parameters (μ, σ^2) , truncated to the right above b .
- 15) Define Laplace distribution with parameters (μ, λ) . Find its m.g.f. and hence mean.
- 16) If $(X, Y) \sim \text{BN}((0, 0, \sigma^2, \sigma^2, \rho))$ then find the distribution of $Z = X/Y$.
- 17) If $(X, Y) \sim \text{BN}((\mu_1, \mu_1, \sigma^2, \sigma^2, \rho))$ then find
 - i) Marginal distribution of Y
 - ii) Conditional distribution of Y given $X = x$

Q.3. Attempt any 04 questions

4 Marks

- 1) Obtain distribution function of Weibull distribution.
- 2) Define Logistic distribution with parameters (μ, σ) and find its mean.
- 3) Define Multinomial distribution and obtain its m.g.f.
- 4) If X follows Pareto distribution with parameters $(1, 2)$ then find $P(X < 3)$.
- 5) Obtain mean and variance of truncated Exponential distribution, truncated to the left below a .
- 6) Prove that independence & uncorrelatedness imply each other of BND.
- 7) Obtain median of Lognormal distribution.

- 8) Obtain mean of truncated Binomial distribution, truncated to the left at $X = 0$.
- 9) If $(X,Y) \sim \text{BN}((\mu_1, \mu_2, \sigma_1^2, \sigma_2^2, p))$ then obtain marginal distribution of X .
- 10) If $(X,Y) \sim \text{BN}((0, 0, 1, 1, p))$ then find the correlation coefficient between X^2 and Y^2 .
- 11) If X follows Laplace distribution with parameters $(\mu=0, \lambda=1)$ then find $P(1 \leq |X| \leq 2)$.
- 12) Find mean of Weibull distribution with parameters (α, β) .
- 13) Define Logistic distribution with parameters (μ, σ) and find its mode.
- 14) If $(X,Y) \sim \text{BN}((\mu_1, \mu_2, \sigma_1^2, \sigma_2^2, p))$ then find conditional distribution of X given $Y = y$.
- 15) Define power series distribution and show that binomial distribution is a particular case of power series distribution.
- 16) Obtain mean of truncated normal distribution, truncated to the right above b , with parameters (μ, σ^2)
- 17) If X follows Cauchy distribution with parameters $(\mu=0, \lambda=1)$ then find the distribution of X^2 .

18) If $(X, Y) \sim \text{BN}(1, 2, 4^2, 5^2, 12/13)$ then find

i) $P(X > 2)$

ii) $P(X > 2 | Y = c)$

Given that $\Phi(0.25) = 0.59871$ and $\Phi(0.65) = 0.74215$ where Φ is the cdf of SNV.

19) A fair die is rolled 6 times. Find the probability that number 1 appear 2 times number 2 or 3 appears 2 times, number 4 or 5 appears 1 time and number 6 appear one time.

20) Obtain the distribution function of the random variable X which follows Laplace distribution with parameters (μ, λ) .

21) State Cumulative distribution function of Cauchy distribution. Hence obtain quartiles.

22) Define truncated exponential distribution, truncated to the left below at $X = A$ also find its mean.

23) Obtain m.g.f. of Laplace distribution.

24) Define Logistic distribution obtain its distribution function.

25) Obtain correlation coefficient for multinomial distribution.

26) In trinomial case obtain its Marginal distribution.

27) State and prove additive property of multinomial distribution.

28) With usual notations obtain mean and variance of Lognormal distribution.

29) Obtain mode of Weibull distribution.

30) A fair die is rolled 12 times, find probability that

i) 1 will occur twice

ii) 3 will occur 3 times

iii) 5 will occur once

iv) 6 will occur twice